

ASSIGNMENT # 1(MTH202)

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Q1: Which of the following are the propositions? Write Truth value of each proposition.

1. Ali is an intelligent boy.	(F)	PREPOOSITION
2. She cooks well.		NOT A PREPOSITION
3. $5 + 6 = 12$	(F)	PREPOOSITION
4. $x + 5 >$		NOT A PREPOOSITION
5. The sun sets in the west.	(T)	PREPOOSITION
6. Complete your homework.		NOT A PREPOOSITION
7. Respect your elders.		NOT A PREPOOSITION
8. The set of natural numbers begins with 1.	(T)	PREPOOSITION
9. The square root of 2 is irrational.	(F)	PREPOOSITION
10. The sky is blue at night.	(F)	PREPOOSITION
11. Honesty is the best policy.	(T)	PREPOOSITION

Q2: Let p = "I am a student of Computer Science."

q = "I work hard."

Then translate the following logical expressions into English sentences.

- $p \rightarrow q$
If i am a student of Computer Science then I must work hard.
- $q \rightarrow p$
If I work hard then I must be Computer Science Student.
- $p \leftrightarrow q$
If I am a student of Computer Science if and only if I work hard.
- $\sim p \rightarrow \sim q$
If I am not a student of Computer Science then I must not work hard.
- $\sim q \rightarrow \sim p$
if I m not working hard then I must not be a Student of Computer Science.
- $\sim (p \rightarrow q)$ Use the result: $\sim (p \rightarrow q) = p \vee \sim q$
I m a student of Computer Science and I don't work hard.

Q3: let h = "Asad is happy."

s = "Asad is sad."

t = "Asad watch television."

Then translate the following logical expressions into English sentences

- $h \rightarrow t \vee \sim s$
if Asad is happy then he watch TV and he is not sad.
- $s \leftrightarrow \sim t$
Asad is sad if and only if he is not watch TV.
- $\sim t \rightarrow \sim h$

If Asad is not watch TV then he is not happy.

- $\sim t \rightarrow h \wedge s$

Asad is not watch TV then he is happy or he is sad.

- $t \wedge h \leftrightarrow \sim s$

Asad watch TV or he is happy if and only if he is not sad.

Q4: Write converse, inverse, contra-positive of the following conditional sentences:

a: If Ali plays soccer, then Bilal plays hockey.

Converse: If Bilal plays hockey, then Ali plays soccer.

Inverse: If Ali not plays soccer, then Bilal is not plays hockey

contra-positive If Bilal not plays hockey, then Ali is not plays soccer.

b: If it is spring season, then trees are green.

Converse: If trees are green, then its spring season.

Inverse: If it is not a spring season, then the trees are not green.

contra-positive If trees are not green, then its not spring season.

c: if x is a natural number, then 2x is an even number.

Converse: If 2x is an even number, then the x is a natural number.

Inverse: If x is not a natural number, then 2x is not an even number.

contra-positive: If 2x is not an even number, then the x is not a natural number.

Q5: Construct the truth table for $\sim (p \rightarrow q)$

(Hint: Use the result : $\sim (p \rightarrow q) = (p \wedge \sim q)$)

p	q	$\sim q$	$p \rightarrow q$	$\sim (p \rightarrow q)$	$(p \wedge \sim q)$
T	T	F	T	F	F
T	F	T	F	T	T
F	T	F	T	F	F
F	F	T	T	F	F

Q6: What is the truth value of each of the following logical expressions ?

Given : p = True, q = False

(For example : $p \vee q = \text{True} \vee \text{False} = \text{True}$)

P	Q	$\sim p$	$\sim q$	$p \wedge q$	$p \vee q$	$\sim (p \wedge q)$	$\sim q \rightarrow \sim p$	$p \rightarrow q$	$\sim q \rightarrow p$	$\sim p \vee \sim q$	$p \leftrightarrow q$
T	F	F	T	F	T	T	T	F	T	T	F